

Original article

# Dynamic behavior of nanometer-scale amorphous intergranular film in silicon nitride by *in situ* high-resolution transmission electron microscopy

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## Abstract

We report about the dynamic behavior of a nanometer-scale amorphous intergranular film (IGF) in a  $\text{Si}_3\text{N}_4$  ceramic by an *in situ* heating experiment in a high-resolution transmission electron microscopy (HRTEM). During the experiment the IGF gradually vanishes at 820 °C accompanied by the formation of crystal planes within the IGF. The IGF reappears after cooling back to room temperature. The results cannot be explained within the framework of a force balance model. We argue that the dynamic behavior of the IGF in our experiment originates from the open system observed. © 2011 Elsevier Ltd. All rights reserved.

**Keywords:**  $\text{Si}_3\text{N}_4$  ceramic; Intergranular amorphous film (IGF); *In situ* HRTEM; Continuum model

## 1. Introduction

As structural materials with outstanding high-temperature properties,  $\text{Si}_3\text{N}_4$ -based ceramics have received much attention and their properties have been studied extensively. As a result of liquid phase sintering, grain boundaries other than low- or special (low  $\Sigma$ ) angle ones, in  $\text{Si}_3\text{N}_4$  ceramics feature amorphous intergranular films (IGF) with a thickness of the order of 1 nm.<sup>1–4</sup> Clarke suggested a continuum model based on a balance of different forces leading to an equilibrium IGF thickness.<sup>5</sup> The major contributions in this model are the attractive van der Waals force, a repulsive steric force, and a potentially present electrical double layer force. It is expected that the magnitude of these forces is determined by compositional changes in the IGF, e.g., the concentration of cationic and anionic sintering additives. Since the composition of sintering additives strongly affects the mechanical properties of the ceramic<sup>6</sup> it is extremely desirable to understand the elemental distribution within the IGF, particularly that of the rare-earths used as sintering additives. This proved experimentally to be a very difficult task. With the advent

of aberration-corrected STEM it seems now to become possible to characterize the detailed atomic structure in such localized IGF volumes using a fine electron probe with a diameter of less than 1 Å.<sup>7–9</sup> First results show that rare-earth dopants preferentially segregate to the (amorphous) film/(crystalline) grain interface.

Industrial interest in structural ceramics is to a large portion due to their excellent high temperature strength and creep resistance. Concluding high-temperature properties from data collected from quenched samples is dangerous, especially, since cooling rates attainable in most experiments are rather slow at temperatures above 1000 °C. It is important to study the behavior of these ceramics at the temperatures they are commonly applied at. However, up to now, only few TEM studies have aimed at investigating the high-temperature structure of IGFs in  $\text{Si}_3\text{N}_4$ , except for *in situ* conventional TEM experiments<sup>10</sup> and studies which use thinned TEM samples quenched from high temperatures.<sup>11</sup> Both fail to faithfully demonstrate the behavior of IGFs at elevated temperature at the atomic-level.

We will show that *in situ* HRTEM experiments are able to reveal the behavior of these materials at high temperature with atomic resolution,<sup>12</sup> reporting first experimental *in situ* HRTEM observations of the evolution of an IGF in  $\text{Si}_3\text{N}_4$  at a temperature of about 820 °C.

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## 2. Experimental methods

A silicon nitride ( $\text{Si}_3\text{N}_4$ ) ceramic doped with 2 wt.%  $\text{MgO} + 7.2$  wt.%  $\text{La}_2\text{O}_3$  was used in this investigation. TEM samples were prepared by grinding, dimpling, polishing and ion milling as the final step. For ion milling an inclination angle of  $12^\circ$  was used. The Ar ion energy was in the range of 2.5–4.0 keV in a Gatan Duomill. The JEOL ARM 1250 microscope with a point-to-point-resolution of 0.12 nm was used for the *in situ* HRTEM studies. The sample was suspended and heated using a Gatan double-tilt heating stage. The microscope is equipped with a drift compensation system, allowing the operator to stabilize the image and record photographs despite thermally induced specimen/stage drift.<sup>13</sup> The *in situ* annealing temperature in these experiments was about  $820^\circ\text{C}$ . The specimen was held at this temperature for about 2 h, and was then cooled back to room temperature within a short time of typically 1 min. To minimize irradiation effects special care was taken when the images were acquired. The specimen was kept at low magnification and with the beam fully spread while being held at high temperature. All the HRTEM images were recorded with exposure times of less than 1 s, and under a defocus which corresponds to the minimum delocalization in this microscope.

## 3. Results and discussion

Fig. 1(a) shows the HRTEM image of two close  $\text{Si}_3\text{N}_4$  particles before heating (the bright-field TEM image is inserted in the center). In the bigger particle,  $\{10\bar{1}0\}$  prism planes are parallel to the interface, while in the smaller one ( $\sim 200$  nm in size) these planes are inclined by  $24^\circ$ . The interface is very sharp and flat. It is obvious that an equilibrium amorphous IGF with a homogeneous thickness of about 1.0 nm exists and both prism planes are flat (the inset shows a diffraction pattern from these two particles, the prism planes of which are strongly excited). Fig. 1(b)–(e) shows the series of *in situ* HRTEM images recorded at elevated temperatures after different annealing times, which clearly show the evolution of the IGF with time. After 30 min the IGF starts to thin until it completely vanishes after 40 min. At the same time additional  $\{10\bar{1}0\}$  lattice planes appear in the interface region on the side of the bigger particle (marked by arrows in Fig. 1(b)–(f)), the number of which increases during the annealing treatment. The size of the smaller particle shrinks which becomes apparent by the shortening of the interface length (compare Fig. 1(a) and (f)). This can be clearly seen in the final stage of the two hours *in situ* annealing (Fig. 1(e)). In order to avoid the very fast drift during cooling (which took about 1–2 min) of the specimen the photograph shown in Fig. 1(f) was acquired about 10 min after having cooled back to room temperature. Note that one additional plane in the interface region has formed during the cooling, which is also found in quenching and annealing investigations.<sup>8,14</sup> Another noticeable feature is that the IGF has reappeared with a thickness of about 0.6 nm when the sample is observed at room temperature again.

In each of the Fig. 1(a)–(f) a cartoon illustrating the development of the additional planes with holding time has been inserted. These additional crystal planes slowly grow as the

annealing proceeds and extend outside the IGF regions. Simultaneously the smaller particle shrinks. The appearance of additional crystal planes in the interface region is probably due to partial crystallization of the IGF during the time spent at high temperature. However, in contrast to previous observations<sup>7,8</sup> the crystallization of the IGF occurred at a relatively low annealing temperature. We also observe that the thickness of the IGF changes remarkably during *in situ* heating. With the software Digital Micrograph, the thickness variation of the nanometer-scale amorphous IGF was measured (Fig. 2). Obviously, holding the sample at high temperature causes a gradual decrease of the IGF thickness, making it disappear eventually, while atomic-level disorder may still be observed at the interface. Compared with the original value (approximately 0.9 nm), the IGF is thinner after cooling back to room temperature.

In order to understand the observed phenomena we will first discuss them in light of Clarke's model,<sup>5,15</sup> showing that our observations cannot be explained using a force balance model based on dispersion- steric- and electrical double layer forces. We will then propose a mechanism based on a changing IGF composition during annealing.

Of all the forces occurring in Clarke's model,<sup>5,15,16</sup> mainly the attractive dispersion force,  $\Pi_{disp}$ , and the repulsive electrical double layer force  $\Pi_{edl}$  have any significant dependence on temperature and may therefore initiate changes in the IGF thickness as the temperature increases. Once the thickness of the film changes the magnitude of all other forces is affected as well. Therefore, to completely evaluate the total force which the IGF is exposed to during heating, its relationship with temperature and IGF thickness must be established.

The attractive dispersion force can be written in the following form<sup>5</sup>:

$$\Pi_{disp} = \frac{H_{\beta g \beta}}{6\pi h^3}$$

$h$  is the thickness of the intergranular film, the Hamaker constant,  $H_{\beta g \beta}$ , for the ceramic system can be expressed in a reduced form in case of a two-grain boundary as shown by Clarke, i.e., two  $\text{Si}_3\text{N}_4$  grains separated by a siliceous amorphous film,

$$H_{\beta g \beta} = \frac{3}{4} k_B T \left( \frac{\varepsilon_\beta - \varepsilon_g}{\varepsilon_\beta + \varepsilon_g} \right)^2 + \frac{3\pi \hbar \nu_e}{8\sqrt{2}} \frac{(n_\beta^2 - n_g^2)^2}{(n_\beta^2 + n_g^2)^{3/2}} \quad (1)$$

where  $\hbar$  is Planck's constant divided by  $2\pi$ ;  $\nu_e$  is the absorption frequency,  $\varepsilon$  and  $n$  are low-frequency dielectric constant and the refractive index, respectively, of the phases  $\beta$  and  $g$  (here, bulk  $\text{Si}_3\text{N}_4$  and intergranular film, respectively),  $k_B$  is the Boltzmann constant,  $T$  is the absolute temperature. By changing the dielectric constants  $\varepsilon$  and indices of refraction  $n$  of the phase  $\beta$  (crystalline) and  $g$  (amorphous IGF), the Hamaker constant  $H_{\beta g \beta}$ , and hence the attractive force across the grain boundary and the film thickness  $h$  are changed as well.

For simplicity, the investigated ceramic system is designated as the  $\beta\text{-Si}_3\text{N}_4\text{-SiO}_2\text{-}\beta\text{-Si}_3\text{N}_4$ . The corresponding parameters of  $\beta\text{-Si}_3\text{N}_4$  and pure  $\text{SiO}_2$  dielectric constant and refractive indices are adopted, which are 2.06 and 8.0 for  $\text{Si}_3\text{N}_4$ , 1.448 and 3.81 for  $\text{SiO}_2$ , respectively.<sup>5</sup> The electronic absorption fre-



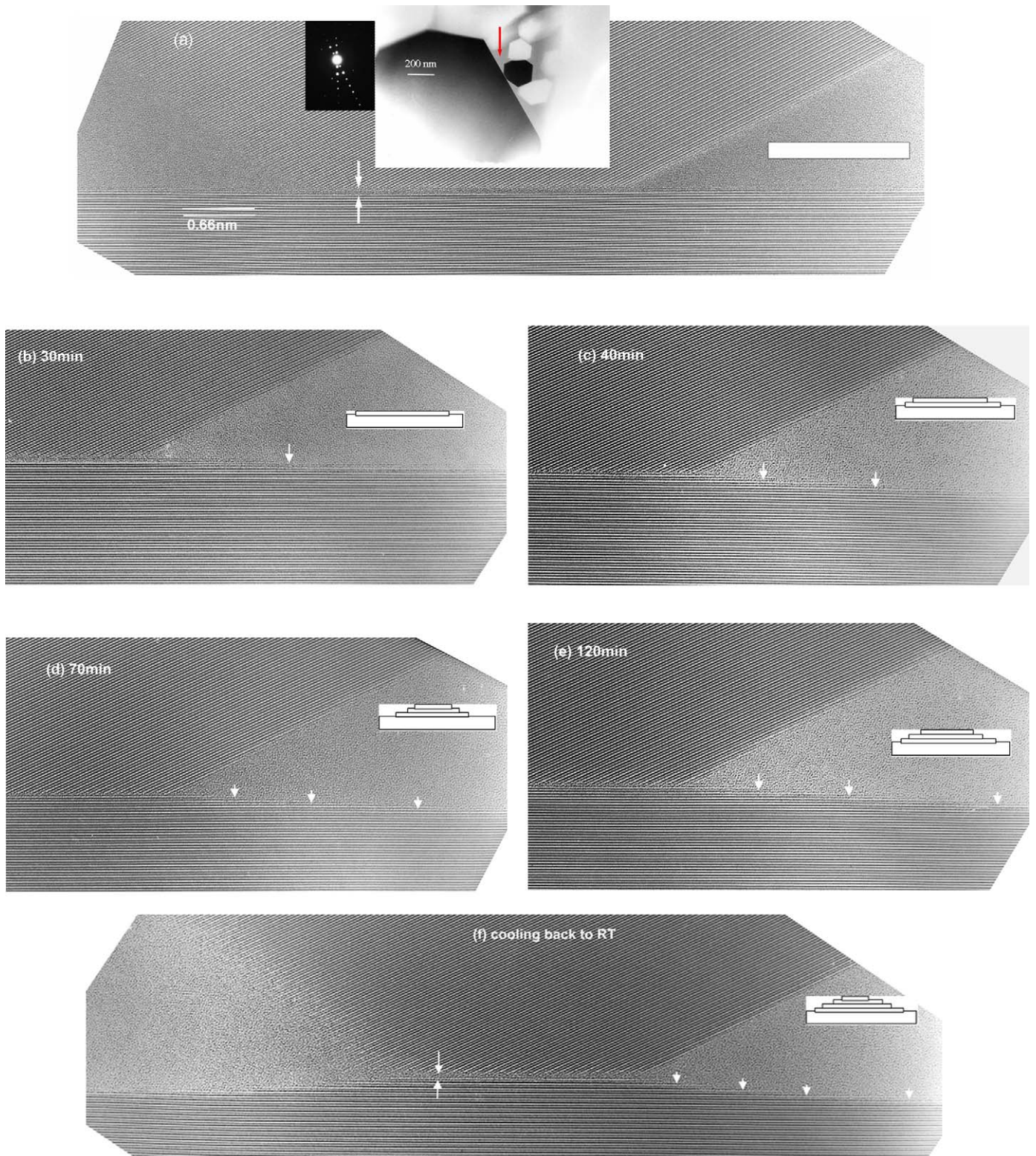


Fig. 1. HRTEM images of an amorphous IGF in  $\text{Si}_3\text{N}_4$ , (a) before heating, (b)–(e) time sequence images during *in-situ* heating at about 820 °C at different holding time. (b) 30min, (c) 40min, (d) 70min, and (e) 120 min. (f) was recorded 10 min after cooling back to room temperature. Note the thickness variation of the IGF with time. Please note that (b)–(e) only show half of the whole image. The bright-field image and corresponding diffraction pattern are inserted in (a). A red arrow in (a) indicates the position where HRTEM images were taken.

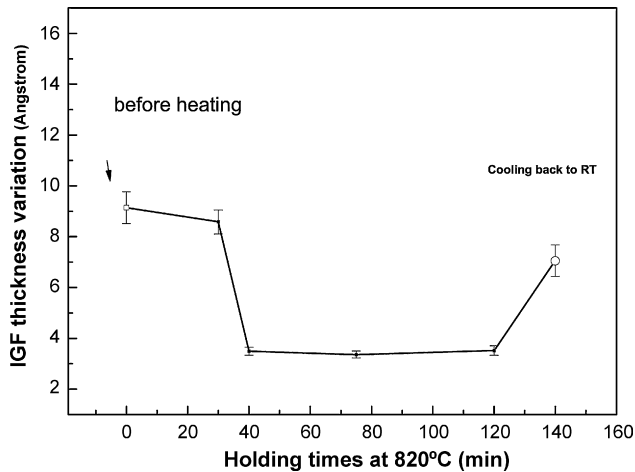


Fig. 2. Variation of the IGF thickness with holding time is displayed. For comparison the values before heating (the first point) and after heating (the last point) are also inserted.

quency is  $\nu = 3 \times 10^{15}$  s.<sup>16</sup> Fig. 3(a) shows a three-dimensional surface plot of the dispersion force as a function of the IGF thickness (from the 0.6 to 1.4 nm) and temperature (from 300 to 2000 K). It indicates that the IGF thickness has relatively strong

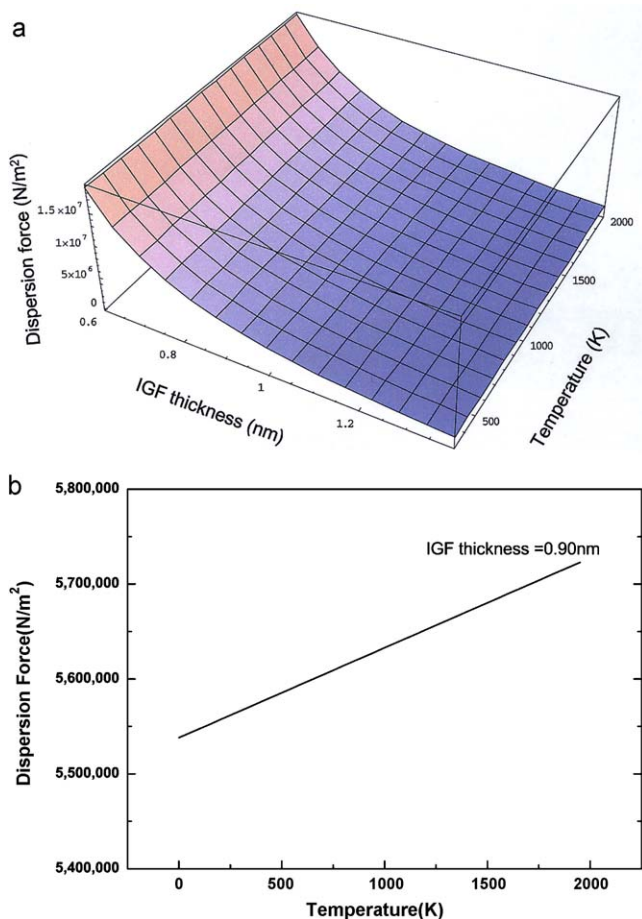


Fig. 3. (a) The estimated dispersion force variation with annealing temperature, from 300 to 2000 K, and IGF thickness from 0.60 to 1.4 nm. (b) Temperature dependence of the dispersion force for an IGF thickness of 0.9 nm, which is close to the experimental condition.

influence on the dispersion force. The linear temperature dependence of the dispersion force is shown enlarged in Fig. 3(b) for an IGF thickness of 0.9 nm. It varies by about 2% between room temperature (RT) and 1150 K. This effect becomes more pronounced at higher temperatures.

Using the weak overlap approximation for the force between charged parallel plates, the repulsive electrical double (EDL) force can be expressed by the following formula which also contains the temperature as a parameter<sup>15,16</sup>

$$\Pi_{edl} = \frac{64(k_B T)^2 \varepsilon \varepsilon_0}{(z e h)^2} \left( \tanh \frac{z e \psi_s}{4 k_B T} \right)^2 \kappa^2 h^2 e^{-\kappa h} \quad (2)$$

with the Debye screening length  $\kappa^{-1} = [(\varepsilon \varepsilon_0 k_B T)/(N z^2 e^2)]^{1/2}$

Here,  $e$  is the proton charge,  $\varepsilon$  is the dielectric constants of the intervening IGF, and  $\varepsilon_0$  is the permittivity of free space,  $z$  is the ion charge,  $\psi_s$  is the electrostatic potential on the surfaces of the grains,  $N$  denotes the number density of mobile ions in the bulk,  $5 \times 10^{-3}$  (number/nm<sup>3</sup>) is used in this system.<sup>17</sup> Based on the assumption underlying Eq. (2), namely a weak double-layer overlap ( $kh > 1$ ), a relatively low surface potential can be suggested. In our estimation  $\psi_s = 100$  mV is assumed. With appropriate parameters the EDL force between two grains can be calculated from Eq. (2). Its variation with IGF thickness and temperature is shown in Fig. 4(a). The increase of the EDL with temperature becomes less pronounced at high temperatures. Although the *relative* influence of the IGF thickness on the EDL force is stronger compared with the dispersion force, the magnitude of the EDL force is at least two orders of magnitude lower than the dispersion forces under the same conditions. Fig. 4(b) plots the dispersion force and the EDL force as functions of IGF thickness at 1150 K and a 100 mV surface potential. This shows how these two forces change as the IGF thickness shrinks during the annealing treatment.

These calculations show that the strongest temperature influence comes from the variation of the dispersion forces which tends to decrease the IGF thickness with increasing temperature. Although this is in accordance with our observations, it has to be noted that within the temperature range studied the variation of forces is so small that this can hardly be the main reason for the observed complete disappearance of the IGF, especially, since the repulsive steric force is proportional to  $\exp(-h/\zeta)$ , where the screening length  $\zeta$  is of the order of  $\approx 3$  Å.<sup>5</sup> We will therefore consider a different mechanism that may be responsible for the changes observed in our experiment.

From Fig. 1(a)–(e) it can be seen that new  $\{10\bar{1}0\}$  crystal planes nucleate within the IGF and further grow, probably by a ledge mechanism, into areas extending outside the IGF region. At the same time, the length of the interface decreases, i.e., the smaller grain loses material at its sides. The tendency for lattice planes to nucleate at the larger grain within the IGF is obviously due to the proximity of the small grain. We believe that the newly forming  $\{10\bar{1}0\}$  planes have a composition close to  $\text{Si}_3\text{N}_4$  because of the same spacing of the newly formed planes as the  $\{10\bar{1}0\}$   $\text{Si}_3\text{N}_4$  planes and because the atoms present in the amorphous phase (e.g., Lu, Mg) have a very low solubility within the  $\text{Si}_3\text{N}_4$  lattice. While this fact alone might classify the



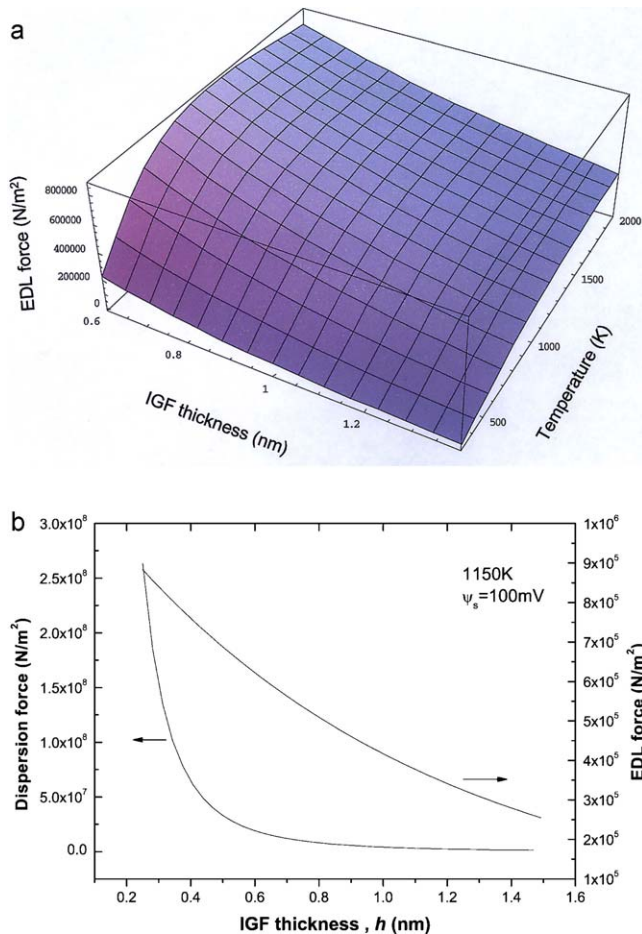


Fig. 4. (a) Electrical double layer (EDL) force as a function of temperature and IGF thickness. (b) Comparison of dispersion force and electrical double layer force at  $T = 1150 \text{ K}$  and for a surface potential of  $100 \text{ mV}$ . Note that the dispersion force is several orders of magnitude larger than the electrical double force.

observation as a classical case of Ostwald ripening (the higher boundary curvature of the smaller grain gives it a higher, less favourable, surface energy density than the large grain), the apparent disappearance of the IGF cannot be explained by it. The crystallization of amorphous material to form new  $\text{Si}_3\text{N}_4$  lattice planes can only occur, if its composition is close to that of the crystal. The atomic species, making up the IGF in its room temperature composition must either (a) concentrate at the IGF center, (b) diffuse along the IGF to the glassy pockets, or (c) spill over the top and/or bottom of the thin TEM sample. It is also conceivable that, despite the special care taken to minimize radiation damage, (d) certain elements have preferentially been removed from the glass by the high-energy electron beam. Any of the described scenarios (a)–(d) affects the composition and therefore the forces across the IGF, and ultimately, its thickness. In our case the interface is about  $28 \text{ nm}$  long and approximately  $10$ – $15 \text{ nm}$  deep in the direction parallel to the electron beam. The scenarios (b) and (c), i.e., diffusion of certain species to the sides and spilling of amorphous phase to the top and/or bottom of the sample are therefore possible and, just from the distance argument, similarly likely. For larger interface areas the diffusion and/or liquid mass flow are less likely under otherwise equal

circumstances. In confined systems, where mass flow is strongly inhibited, crystallization as observed in our experiment is also more difficult, since volume changes associated with the phase transformation give rise to strain energy.<sup>18</sup>

A simple entropic argument will easily discount possibility (a), the concentration of elements other than Si and N to the very center of the IGF. Scenario (d) may be the most likely, if it can be shown that La, O, and possibly Mg are removed more easily by the electron beam than Si and N. While Si and N have 4 and 3 bonds, oxygen atoms are only bound twice, and La atoms feel more comfortable at the  $\text{Si}_3\text{N}_4$ /IGF interface than in the center of the IGF.<sup>7,9</sup> Electron beam damage of the IGF may therefore preferentially remove the comparatively weakly bound oxygen atoms, leaving behind positively charged  $\text{La}^{3+}$ ,  $\text{Mg}^{2+}$ ,  $\text{Si}^{4+}$ , and  $\text{N}^{3+}$ , the latter 2 of which form  $\text{Si}_3\text{N}_4$  (together with the material dissolved off the smaller grain). The remaining positively charged ions repel each other and move to the specimen surfaces and/or are also knocked out of the thin TEM foil by electron beam. The availability of equivalent low-energy sites makes knock-on electron beam damage less likely for crystallizing and already crystallized regions of the sample, leaving behind a (possibly just partially) crystallized IGF.

The re-appearance of the IGF while cooling back to room temperature may be explained in a similar fashion as its disappearance. Temperature induced compositional changes by diffusion and mass flow (possible explanations (b) and (c)) are reversible. The reduced IGF thickness after cooling down may be kinetically limited, i.e., a result of the relatively fast cooling rate, compared to the time it took the IGF to disappear. If radiation damage was responsible for the IGF thinning, diffusion from the glassy pockets must have filled the interface again. In ceramics containing neither magnesium, nor rare earth oxide additives Tanaka et al. found the IGF width to be  $(1.0 \pm 0.1) \text{ nm}$ ,<sup>2</sup> which is significantly less than the with  $(1.6 \pm 0.1) \text{ nm}$  commonly quoted for  $\text{La}_2\text{O}_3$ -doped material.<sup>3</sup> Permanent removal of oxygen and the (by charge balance) corresponding amount of anions may have led to a different composition and thus a smaller thickness of the IGF after cooling down.

#### 4. Conclusion

In summary, with *in situ* HRTEM it has been shown that an amorphous IGF can vanish at elevated temperature by the occurrence of additional crystal planes in the interface region during annealing, and that the IGF can reoccur after cooling back to room temperature. These results are different from the Clarke's<sup>10</sup> and Cinibulk's<sup>11</sup> observations, who claimed that no observable changes in the secondary phases at triple junctions or along grain boundary occur below  $1000 \text{ }^\circ\text{C}$ . From the analysis of the forces assumed, according to Clarke's model,<sup>5,15</sup> to be acting upon the grains confining the amorphous IGF we concluded that their temperature dependence is too small to explain the variation of IGF thickness. Alternative explanations based on alteration of the IGF composition during annealing have been proposed. In addition, mass transport was observed to occur from smaller to larger grains.

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